

同时具有状态与控制时变时滞系统的 H_∞ 输出反馈控制 *

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摘要: 针对同时具有状态与控制时变时滞的线性系统, 基于代数 Riccati 方程方法, 给出了一个 H_∞ 输出反馈控制器设计方案. 该方案既能使闭环系统稳定, 又能保证系统具有一定的 H_∞ 性能.

关键词: H_∞ 输出反馈控制; 代数 Riccati 方程; 时变时滞

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H_∞ Control via Output Feedback for Linear Systems with Time-Varying Delayed State and Control

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Abstract: Based on algebraic Riccati equation, this paper provides a design scheme of H_∞ output feedback controller aimed at linear systems with time-varying delayed state and control, which can stabilize the systems and guarantee a prescribed H_∞ performance.

Key words: H_∞ control via output feedback; algebraic Riccati equation; time-varying delays

1 引言 (Introduction)

在实际工程系统中, 由于信号的传递和观测需要时间以及被控对象的元件老化等原因, 时滞现象普遍存在. 近年来已提出许多有用的技术以分析时滞系统的性能和稳定性, 其中 H_∞ 控制技术倍受关注^[1-16].

时滞系统的 H_∞ 状态反馈控制研究已取得较大进展. 1994 年 Lee 等^[1]通过求解代数 Riccati 方程, 给出了一个无记忆 H_∞ 状态反馈控制器用于状态时滞系统. 1995 年, Choi 和 Chung^[2]讨论了同时具有状态和控制时滞的线性时不变系统的 H^∞ 状态反馈控制问题. 1998 年, Su 等^[3]讨论了带时变状态与控制时滞的时变不确定系统的情况. 在时滞系统的 H_∞ 输出反馈控制方面, 1996 年, Ge 等^[4]提出了状态时滞系统的 H_∞ 输出反馈控制问题, Jeung 等^[5]考虑了时变状态时滞的情况, 1997 年, Choi 和 Chung^[6]采用 Riccati 方程方法, 提出了一个基于观测器的鲁棒 H_∞ 控制, 用于带有界时变不确定性的线性时滞系统. 但是目前对同时具有状态与控制时滞系统的 H_∞ 输出反馈控制问题还未见探讨.

本文针对同时具有状态与控制时变时滞的线性系统, 基于代数 Riccati 方程方法, 设计 H_∞ 输出反馈控制器, 使闭环系统稳定, 且满足 $\|z(t)\|_2 < \gamma \|w(t)\|_2$.

2 H_∞ 输出反馈控制 (H_∞ control via output feedback)

本文考虑如下同时具有状态与控制时变时滞的系统:

$$\begin{cases} \dot{x}(t) = Ax(t) + A_d x(t - \tau_1(t)) + B_1 w(t) + B_2 u(t) + B_d u(t - \tau_2(t)), \\ z(t) = C_1 x(t) + D_{11} w(t) + D_{12} u(t), \\ y(t) = C_2 x(t) + D_{21} w(t), \\ x(t) = 0, t \leq 0. \end{cases} \quad (1)$$

式中, $x(t) \in \mathbb{R}^n$ 为系统状态, $w(t) \in \mathbb{R}^q$ 为干扰输入, $u(t) \in \mathbb{R}^m$ 为控制输入, $z(t) \in \mathbb{R}^{p_1}$ 为系统控制输出, $y(t) \in \mathbb{R}^{p_2}$ 为测量输出, $A, B_1, B_2, A_d, B_d, C_1, C_2, D_{11}, D_{12}, D_{21}$ 是具有适当维数的常矩阵, $\tau_1(t), \tau_2(t)$ 分别为状态和控制时变时滞, 且满足下列假设:

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$$0 \leq \tau_1(t) < \tau_1 < \infty, \tau_1(t) \leq d_{\tau_1} < 1, \quad (2)$$

$$0 \leq \tau_2(t) < \tau_2 < \infty, \tau_2(t) \leq d_{\tau_2} < 1. \quad (3)$$

对于系统(1),采用以下输出反馈控制:

$$\begin{cases} \dot{x}_c(t) = A_c x_c(t) + B_c y(t), \\ u(t) = C_c x_c(t), \\ x_c(t) = 0, t \leq 0. \end{cases} \quad (4)$$

式中, $x_c(t) \in \mathbb{R}^n$ 是控制器状态, A_c, B_c, C_c 是控制器参数.

闭环系统可表示为:

$$\begin{cases} \begin{bmatrix} \dot{x}(t) \\ \dot{x}_c(t) \end{bmatrix} = \begin{bmatrix} A & B_2 C_c \\ B_c C_2 & A_c \end{bmatrix} \begin{bmatrix} x(t) \\ x_c(t) \end{bmatrix} + \begin{bmatrix} A_d & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x(t-\tau_1) \\ x_c(t-\tau_1) \end{bmatrix} + \\ \begin{bmatrix} 0 & B_d C_c \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x(t-\tau_2) \\ x_c(t-\tau_2) \end{bmatrix} + \begin{bmatrix} B_1 \\ B_c D_{21} \end{bmatrix} w(t), \\ z(t) = [C_1 \quad D_{12} C_c] \begin{bmatrix} x(t) \\ x_c(t) \end{bmatrix} + D_{11} w(t). \end{cases} \quad (5)$$

取坐标变换阵 $T = \begin{bmatrix} I & 0 \\ I & -I \end{bmatrix}$, 则闭环系统(5)

可转化为:

$$\begin{cases} \dot{\eta}(t) = A_d \eta(t) + A_{cd} \eta(t - \tau_1(t)) + \\ B_{cd} C_{cd} \eta(t - \tau_2(t)) + B_c w(t), \\ z(t) = C_d \eta(t) + D_d w(t), \\ \eta(t) = 0, t \leq 0. \end{cases} \quad (6)$$

其中

$$\begin{aligned} \eta(t) &= \begin{bmatrix} x(t) \\ x(t) - x_c(t) \end{bmatrix}, \\ A_d &= \begin{bmatrix} A + B_2 C_c & -B_2 C_c \\ A + B_2 C_c - B_c C_2 - A_c & A_c - B_2 C_c \end{bmatrix}, \\ A_{cd} &= \begin{bmatrix} A_d & 0 \\ A_d & 0 \end{bmatrix}, B_{cd} = \begin{bmatrix} B_d \\ B_d \end{bmatrix}, \\ C_{cd} &= [C_c \quad -C_c], B_c = \begin{bmatrix} B_1 \\ B_1 - B_c D_{21} \end{bmatrix}, \\ C_d &= [C_1 + D_{12} C_c \quad -D_{12} C_c], D_d = D_{11}. \end{aligned}$$

为方便定理证明,引入以下两个引理:

引理 1^[13] 对具有适当维数的矩阵 X, Y , 任取常数 $\alpha > 0$, 有下式成立:

$$X^T Y + Y^T X \leq \frac{1}{\alpha} X^T X + \alpha Y^T Y.$$

引理 2^[17] 对具有适当维数的矩阵 F, G , 有下式成立:

$$(I - FG)^{-1} = I + F(I - GF)^{-1}G.$$

定理 1 对常数 $\alpha_1 > 0, \alpha_2 > 0$, 若有 $\gamma^2 I -$

$D_{cd}^T D_{cd} > 0$, 且存在正定对称阵 $P > 0$ 满足下式:

$$\begin{aligned} S &= A_d^T P + P A_d + C_{cd}^T C_{cd} + \\ & (P B_d + C_{cd}^T D_d) (\gamma^2 I - D_{cd}^T D_{cd})^{-1} (B_d^T P + D_{cd}^T C_{cd}) + \\ & \frac{P A_{cd} A_{cd}^T P}{\alpha_1 (1 - d_{\tau_1})} + \alpha_1 I + \frac{P B_{cd} B_{cd}^T P}{\alpha_2 (1 - d_{\tau_2})} + \alpha_2 C_{cd}^T C_{cd} < 0, \end{aligned} \quad (7)$$

则闭环系统(6)渐近稳定, 并且满足 $\|z(t)\|_2 < \gamma \|w(t)\|_2$.

证 对闭环系统(6), 取 Lyapunov 泛函为如下形式:

$$\begin{aligned} V(\eta(t), t) &= \eta^T(t) P \eta(t) + \alpha_1 \int_{t-\tau_1(t)}^t \eta^T(\tau) \eta(\tau) d\tau + \\ & \alpha_2 \int_{t-\tau_2(t)}^t \eta^T(\tau) C_{cd}^T C_{cd} \eta(\tau) d\tau > 0, \end{aligned} \quad (8)$$

则有:

$$\begin{aligned} \dot{V}(\eta(t), t) &= \\ & \eta^T(t) A_d^T P \eta(t) + \eta^T(t - \tau_1(t)) A_{cd}^T P \eta(t) + \\ & \eta^T(t - \tau_1(t)) C_{cd}^T B_{cd}^T P \eta(t) + w^T(t) B_c^T P \eta(t) + \\ & \eta^T(t) P A_{cd} \eta(t) + \eta^T(t) P A_{cd} \eta(t - \tau_1(t)) + \\ & \eta^T(t) P B_{cd} C_{cd} \eta(t - \tau_2(t)) + \eta^T(t) P B_c w(t) + \\ & \alpha_1 \eta^T(t) \eta(t) - \alpha_1 (1 - d_{\tau_1}(t)) \eta^T(t - \tau_1(t)) \eta(t - \tau_1(t)) + \\ & \alpha_2 \eta^T(t) C_{cd}^T \eta(t) - \alpha_2 (1 - d_{\tau_2}(t)) \eta^T(t - \tau_2(t)) C_{cd}^T C_{cd} \eta(t - \tau_2(t)). \end{aligned} \quad (9)$$

由式(2), (3)和引理 1 可得:

$$\begin{aligned} \dot{V}(\eta(t), t) &\leq \\ & \eta^T(t) \left[A_d^T P + P A_d + \frac{P A_{cd} A_{cd}^T P}{\alpha_1 (1 - d_{\tau_1})} + \alpha_1 I + \right. \\ & \left. \frac{P B_{cd} B_{cd}^T P}{\alpha_2 (1 - d_{\tau_2})} + \alpha_2 C_{cd}^T C_{cd} \right] \eta(t) + \\ & w^T(t) B_c^T P \eta(t) + \eta^T(t) P B_c w(t). \end{aligned} \quad (10)$$

①考虑稳定性时, 令 $w(t) = 0$, 则由式(10)可得:

$$\begin{aligned} \dot{V}(\eta(t), t) &\leq \\ & \eta^T(t) \left[A_d^T P + P A_d + \frac{P A_{cd} A_{cd}^T P}{\alpha_1 (1 - d_{\tau_1})} + \right. \\ & \left. \alpha_1 I + \frac{P B_{cd} B_{cd}^T P}{\alpha_2 (1 - d_{\tau_2})} + \alpha_2 C_{cd}^T C_{cd} \right] \eta(t). \end{aligned}$$

由式(7)可知: $\dot{V}(\eta(t), t) < 0$, 所以闭环系统(6)渐近稳定.

②定义

$$J = \int_0^\infty [z^T(t) z(t) - \gamma^2 w^T(t) w(t) + \dot{V}(\eta(t), t)] dt.$$

将式(6),(10)代入可得:

$$J \leq \int_0^{\infty} [\eta^T(t) S \eta(t) - T^T (\gamma^2 I - D_{cl}^T D_{cl})^{-1} T] dt,$$

其中

$$T = (B_{cl}^T P + D_{cl}^T C_{cl}) \eta(t) - (\gamma^2 I - D_{cl}^T D_{cl}) w(t).$$

由式(7)可知: $J < 0$. 因系统(6)是渐近稳定, 故 $V(\eta(\infty), \infty) = 0$, 且由式(6)零初始条件可知: $V(\eta(0), 0) = 0$. 所以:

$$\int_0^{\infty} z^T(t) z(t) dt < \gamma^2 \int_0^{\infty} w^T(t) w(t) dt,$$

即:

$$\|z(t)\|_2 < \gamma \|w(t)\|_2.$$

3 H_{∞} 输出反馈控制器设计 (H_{∞} output feedback controller design)

根据定理 1, 以下给出同时具有状态与控制时变时滞的线性系统存在 H_{∞} 输出反馈控制的充分条件.

定理 2 对于系统(1)及任意常数 $\alpha_1 > 0, \alpha_2 > 0$, 若 $\gamma^2 I - D_{11}^T D_{11} > 0$ 成立, 且满足下列条件:

① 存在正定对称矩阵 $X > 0$ 使得:

$$\begin{aligned} & A_F^T X + X A_F + C_F^T C_F + (X B_1 + \\ & C_F^T D_{11}) \Omega_1 (B_1^T X + D_{11}^T C_F) + \frac{X A_d A_d^T X}{\alpha_1 (1 - d_{\tau_1})} + \alpha_1 I + \\ & \frac{X B_d B_d^T X}{\alpha_2 (1 - d_{\tau_2})} + \alpha_2 X B_2 B_2^T X < 0. \end{aligned} \quad (11)$$

其中 $A_F = A - B_2 F, C_F = C_1 - D_{12} F, F = B_2^T X, \Omega_1 = (\gamma^2 I - D_{11}^T D_{11})^{-1}$.

② 存在正定对称矩阵 $Y > 0$, 使得:

$$\begin{aligned} & Y A_G^T + A_G Y + B_G B_G^T + (Y C_1^T + B_G D_{11}^T) \Omega_2 (C_1 Y + D_{11} B_G^T) + \\ & \frac{\gamma^2 A_d A_d^T Y}{\alpha_1 (1 - d_{\tau_1})} + \frac{2\alpha_1 Y Y}{\gamma^2} + \frac{\gamma^2 B_d B_d^T}{\alpha_2 (1 - d_{\tau_2})} < 0. \end{aligned} \quad (12)$$

其中 $A_G = A - G C_2, B_G = B_1 - G D_{21}, G = Y C_2^T, \Omega_2 = (\gamma^2 I - D_{11} D_{11}^T)^{-1}$.

③ $\gamma^2 Y^{-1} > X$. (13)

则存在输出反馈控制(4)使闭环系统(6)渐近稳定, 且满足 $\|z(t)\|_2 < \gamma \|w(t)\|_2$.

满足上述条件的一组输出反馈控制器为:

$$C_c = -B_2^T X, \quad (14)$$

$$B_c = \gamma^2 (\gamma^2 Y^{-1} - X)^{-1} C_2^T, \quad (15)$$

$$\begin{aligned} A_c = & A_F - B_c C_2 + \frac{A_d A_d^T X}{\alpha_1 (1 - d_{\tau_1})} + \frac{B_d B_d^T X}{\alpha_2 (1 - d_{\tau_2})} - \\ & (\gamma^2 Y^{-1} - X)^{-1} M. \end{aligned} \quad (16)$$

其中

$$\begin{aligned} M = & C_c^T B_2^T X + C_c^T D_{12}^T C_F + \alpha_2 C_c^T C_c + \\ & H + [(\gamma^2 Y^{-1} - X)(B_c D_{21} - B_1) + \\ & C_c^T D_{12}^T D_{11}] \Omega_1 (B_1^T X + D_{11}^T C_F), \\ H = & -A_F^T X - X A_F - C_F^T C_F - (X B_1 + \\ & C_F^T D_{11}) \Omega_1 (B_1^T X + D_{11}^T C_F) - \frac{X A_d A_d^T X}{\alpha_1 (1 - d_{\tau_1})} - \\ & \alpha_1 I - \frac{X B_d B_d^T X}{\alpha_2 (1 - d_{\tau_2})} - \alpha_2 X B_2 B_2^T X > 0. \end{aligned} \quad (17)$$

证 选择正定对称矩阵 P :

$$P = \begin{bmatrix} X & 0 \\ 0 & \gamma^2 Y^{-1} - X \end{bmatrix} > 0.$$

定义 $S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$,

其中, $S_{11}, S_{12}, S_{21}, S_{22} \in \mathbb{R}^{n \times n}, S_{12} = S_{21}^T$.

则式(7)可分解成:

$$S_{11} = A_F^T X + X A_F + (X B_1 + C_F^T D_{11}) \Omega_1 (B_1^T X + D_{11}^T C_F) +$$

$$C_F^T C_F + \frac{X A_d A_d^T X}{\alpha_1 (1 - d_{\tau_1})} + \alpha_1 I + \frac{X B_d B_d^T X}{\alpha_2 (1 - d_{\tau_2})} + \alpha_2 C_c^T C_c,$$

$$\begin{aligned} S_{12} = & (A_F - B_c C_2 - A_c)^T (\gamma^2 Y^{-1} - X) - X B_2 C_c - \\ & C_F^T D_{12} C_c + (X B_1 + C_F^T D_{11}) \Omega_1 [(B_1^T - \\ & D_{12}^T B_c^T) (\gamma^2 Y^{-1} - X) - D_{11}^T D_{12} C_c] + \\ & \frac{X A_d A_d^T (\gamma^2 Y^{-1} - X)}{\alpha_1 (1 - d_{\tau_1})} + \frac{X B_d B_d^T (\gamma^2 Y^{-1} - X)}{\alpha_2 (1 - d_{\tau_2})} - \alpha_2 C_c^T C_c, \end{aligned}$$

$$\begin{aligned} S_{22} = & (A_c - B_2 C_c)^T (\gamma^2 Y^{-1} - X) + (\gamma^2 Y^{-1} - \\ & X) (A_c - B_2 C_c) + C_c^T D_{12}^T D_{12} C_c + [(\gamma^2 Y^{-1} - \\ & X) (B_1 - B_c D_{21}) - C_c^T D_{12}^T D_{11}] \Omega_1 [(B_1^T - \\ & D_{12}^T B_c^T) (\gamma^2 Y^{-1} - X) - D_{11}^T D_{12} C_c] + \alpha_1 I + \alpha_2 C_c^T C_c + \\ & \frac{(\gamma^2 Y^{-1} - X) A_d A_d^T (\gamma^2 Y^{-1} - X)}{\alpha_1 (1 - d_{\tau_1})} + \frac{(\gamma^2 Y^{-1} - X) B_d B_d^T (\gamma^2 Y^{-1} - X)}{\alpha_2 (1 - d_{\tau_2})}. \end{aligned}$$

若按式(14)选择控制器参数 C_c , 由式(11), (17)可知: $S_{11} = -H < 0$.

若按式(16), (15)选择控制器参数 A_c, B_c , 并由式(17)可得:

$$\begin{aligned} S_{12} = & S_{21} = H > 0, \\ S_{22} = & \gamma^2 A_G^T Y^{-1} + \gamma^2 Y^{-1} A_G + C_1^T C_1 + 2\alpha_1 I + \\ & \frac{\gamma^4 Y^{-1} A_d A_d^T Y^{-1}}{\alpha_1 (1 - d_{\tau_1})} + \frac{\gamma^4 Y^{-1} B_d B_d^T Y^{-1}}{\alpha_2 (1 - d_{\tau_2})} - H + \\ & (\gamma^2 Y^{-1} B_G + C_1^T D_{11}) \Omega_1 (\gamma^2 Y^{-1} B_G + C_1^T D_{11})^T. \end{aligned} \quad (18)$$

根据引理 2, 有:

$$(\gamma^2 - D_{11}^T D_{11})^{-1} = \gamma^{-2} [I + D_{11}^T (\gamma^2 I - D_{11} D_{11}^T)^{-1} D_{11}].$$

则式(18)可化为:

$$\begin{aligned} S_{22} &= \gamma^2 A_G^T Y^{-1} + \gamma^2 Y^{-1} A_G + \gamma^2 Y^{-1} B_G B_G^T Y^{-1} + 2a_1 I + \\ &\quad \frac{\gamma^4 Y^{-1} A_d A_d^T Y^{-1}}{a_1(1-d_{\tau_1})} + \frac{\gamma^4 Y^{-1} B_d B_d^T Y^{-1}}{a_2(1-d_{\tau_2})} - H + \\ &\quad \gamma^2 (Y^{-1} B_G D_{11}^T + C_1^T) \Omega_2 (Y^{-1} B_G D_{11}^T + C_1^T)^T = \\ &\quad \bar{S}_{22} - H, \\ \bar{S}_{22} &= \gamma^2 Y^{-1} [Y A_G^T + A_G Y + B_G B_G^T + \\ &\quad (Y C_1^T + B_G D_{11}^T) \Omega_2 (Y C_1^T + B_G D_{11}^T)^T + \\ &\quad \frac{\gamma^2 A_d A_d^T}{a_1(1-d_{\tau_1})} + \frac{2a_1 Y Y}{\gamma^2} + \frac{\gamma^2 B_d B_d^T}{a_2(1-d_{\tau_2})}] Y^{-1}. \end{aligned}$$

由式(12)可知:

$$\bar{S}_{22} < 0.$$

则有:

$$\begin{aligned} \begin{bmatrix} I & 0 \\ I & I \end{bmatrix} S \begin{bmatrix} I & I \\ 0 & I \end{bmatrix} &= \\ \begin{bmatrix} I & 0 \\ I & I \end{bmatrix} \begin{bmatrix} -H & H \\ H & \bar{S}_{22} - H \end{bmatrix} \begin{bmatrix} I & I \\ 0 & I \end{bmatrix} &= \begin{bmatrix} -H & 0 \\ 0 & \bar{S}_{22} \end{bmatrix} < 0, \end{aligned}$$

所以 S 负定. 证毕.

4 设计实例(Example)

设一个同时具有状态与控制时变时滞系统(1)的参数如下:

$$\begin{aligned} A &= \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix}, B_1 = \begin{bmatrix} 0 \\ 0.1 \end{bmatrix}, B_2 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \\ A_d &= \begin{bmatrix} 0 & 0 \\ 0.2 & 0.1 \end{bmatrix}, B_d = \begin{bmatrix} 0.1 \\ 0 \end{bmatrix}, \\ C_1 &= [0 \ 1], C_2 = [0 \ 1], \\ D_{11} &= 0.2, D_{12} = 0.5, D_{21} = 0.2, \\ \tau_1(t) &= 2 + 0.5 \sin(t), \tau_2(t) = 3 + 0.3 \cos(t), \\ d_{\tau_1} &= 0.5, d_{\tau_2} = 0.3. \end{aligned}$$

由于式(11)和(12)是不等式,我们选择 $Q_1 = 10^{-5}I$, $Q_2 = 10^{-5}I$ 分别使不等式(11),(12)成为等式,并取 $a_1 = 1$, $a_2 = 1$, 利用 MATLAB 语言求得次优解为:

$$\gamma_{opt} = 0.2838.$$

此时相应的 Riccati 方程的解为:

$$X = \begin{bmatrix} 2.0705 & 0.4614 \\ 0.4614 & 0.7159 \end{bmatrix}, Y = \begin{bmatrix} 0.0202 & -0.0067 \\ -0.0067 & 0.0191 \end{bmatrix}.$$

控制器参数为:

$$A_c = \begin{bmatrix} 0.0152 & 1.1288 \\ -1.4317 & -2.0805 \end{bmatrix},$$

$$B_c = \begin{bmatrix} -0.0104 \\ 0.0227 \end{bmatrix}, C_c = [-0.4614 \quad -0.7159].$$

5 结论(Conclusion)

本文针对同时具有状态与控制时变时滞的线性系统,给出了使整个闭环系统稳定并使其满足 $\|z(t)\|_2 < \gamma \|w(t)\|_2$ 的基于代数 Riccati 方程的解,通过求解两个代数 Riccati 方程即可得到 H^∞ 输出反馈控制器.该方法的一个特点是这两个代数 Riccati 方程可以独立求解.本文仅研究同时具有状态与控制时变时滞的线性系统,对同时具有状态与控制时滞的不确定时变系统的 H^∞ 输出反馈控制问题将进一步研究.

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